

# Quality externalities in credit markets: a case for taxing banks?

Christian Bauer & José V. Rodríguez Mora

November 14, 2011

# Summary



- Quality externalities in credit markets
- Externalities: increasing bank quality
- Model
- Key statistics
- Avg. prob of good project in applicant pool
- Final ingredients
- Value after applying for  $t$  periods, exit at  $R$
- Avg. applicant quality determined by  $w$
- Terms of trade: payment to E
- Value of Bs and free entry
- Recapturing and solving
- Efficiency measure: GDP
- Model in action: efficiency showdown
- Conclusions and outlook
- Backup
- “Wage” determination: no discounting
- “Wage” determination: with discounting



- this is very much (exciting) work in progress
- contribute to understanding inefficiencies in banking activities
- study externalities from investments in quality of banks
  - bank quality: ability to evaluate projects of different quality
  - project quality: ability to generate profit (“productivity”)
  - externalities: on other banks through pool of credit applicants

- **reduces applicant quality** – mechanical response
  - good projects extracted faster
  - negative externality on other banks (tax?)
  - excessive rents in OTC markets (Bolton/Santos/Scheinkman 2011)
  
- **raises applicant quality** – behavioral response\*
  - improves information extraction from time on market
  - update beliefs about project quality using duration of application
  - better bank quality speeds up learning, exit (“paper submission”)
  - faster exit of (on avg.) bad applicants raises avg. quality
  - positive externality on the other banks (subsidy?)

\*our contribution

which dominates? – should we tax or subsidize bank activity?

- entrepreneurs (E), banks (B)
  - Es generate blueprints, look for financing – in frictional market
  - linear utility, continuous time, benchmark model: no discounting
- mass 1 of Es
  - get new project at cost  $F$
  - project is good (g) with prob  $p$ , bad (b) ow.
  - E does not know type ( $\Rightarrow$  a productive role for Bs)
- free entry for Bs
  - B invest in evaluation technology (signal on project quality)
  - B does not know history of E's project

- credit application
  - E applies for credit, but not “called” instantaneously
  - contagion on Bs desks (endog. prob of being evaluated)
  - when B looks at project: signal on quality with prob  $a$  – or not
- get signal, reveals truth – good project:
  - B, E negotiate contract, execute project
  - 1 unit of output, at capital cost  $k$  (instantaneous production)
  - $p < k$  (no production without Bs)
- no signal: no information revealed
- no signal AND negative signal: E NOT INFORMED
  - important: state of E is duration of search w/o receiving signal...

- ...a reasonable simplification
  - alternative: state is number of negative signals. complex.
  - continuous state variable makes life easy (as in Blanchard OLGs)

**bottom line: state is informative on how likely project is bad**

- the longer you are around, the less likely your project is good
- matching technology
  - benchmark: no real search (no search/time costs) – pure info friction
  - with  $b$  banks,  $B$  meets project at rate

$$h(b), \quad h' < 0$$

- projects meet Bs at rate

$$m(b) = bh(b), \quad m' > 0$$

- define **maximum time that E looks for B (endog.):  $R$**
- Es pay  $F$ , start new project whenever
  - drop old project w/o having obtained credit (after  $R$  periods)
  - E obtains credit (instantaneous cookies)



- posterior prob of good project after  $t$  periods

$$Q(t) = \text{Prob}(g|t) = \frac{p e^{-m(b)at}}{\underbrace{1-p}_{\text{Prob}(b)} \times \underbrace{\text{Prob}(t|b)} + \underbrace{p}_{\text{Prob}(g)} \underbrace{e^{-m(b)at}}_{\text{Prob}(t|g)}}$$

- avg. prob of good project in pool of applicants  $\bar{p}$ 
  - equals avg. prob of good project at exit
  - # E's arriving at R b/c not called if good
  - all: them + # arrive at R because bad



$$\frac{\bar{p}}{1 - \bar{p}} = \frac{p}{1 - p} f(\underbrace{\alpha}_{(-)}), \quad \alpha \equiv m(b) \times a \times R$$

- Raising  $a$  (better evaluation)
  - direct effect: **reduces avg. productivity**
  - but: infer faster that project is bad when evaluation is accurate!

$$\Rightarrow R = R(\underbrace{a}_{(-)})$$

- indirect effect:  $R$  falls, **raises avg. productivity**
- equilibrium impact on  $b$

# Final ingredients

---



- determination of exit duration  $R$ 
  - requires value of  $E$
- terms of trade: payment or “wage”  $w$
- close model: free entry into banking
  - requires value of  $B$

# Value after applying for $t$ periods, exit at $R$



$$\begin{aligned} E(t, R) &= [1 - Q(t)] [E(0, R) - F] \\ &+ Q(t) \left[ 1 - \int_t^R m(b) a e^{-m(b)as} ds \right] [E(0, R) - F] \\ &+ Q(t) \left[ \int_t^R m(b) a e^{-m(b)as} ds \right] \{w + [E(0, R) - F]\} \end{aligned}$$

- Recall  $Q(t)$ : belief that project is good at “age”  $t$
- $m(b) a e^{-m(b)as}$ : inst. density that  $g$  is selected after exactly  $s$  periods
- at  $t = 0$  we determine

$$m(b) \times a \times R = \ln \frac{p \times w}{p \times w - F} \quad \text{Cool! Why?! ...}$$

## Avg. applicant quality determined by $w$ (1/2)



$$\frac{\bar{p}}{1 - \bar{p}} = \frac{p}{1 - p} \ln \frac{\frac{F}{pw}}{pw - F}$$

- depends exclusively on E's behavior
  - cost to start a project ( $F$ )
  - how much E may hope to get out of project ( $pw$ )
- irrelevant: rate at which agents meet
  - only b/c no discounting
- Blanchardish design to get block recursive structure/analytical results



$$\frac{\bar{p}}{(1 - \bar{p})} = \frac{p}{1 - p} \frac{\frac{F}{pw}}{\ln \frac{pw}{pw - F}}$$

- $F = 0 \Rightarrow \bar{p} = p$ 
  - E start new project at every instant when not selected
- $F > 0 \Rightarrow \bar{p} < p$ 
  - not selected E (more likely to be bad) take time in exiting
- $pw \uparrow \Rightarrow \bar{p} \uparrow$ 
  - raises incentive to start new project given info that project is bad
  - not selected for some time:  $pw \uparrow \Rightarrow R \downarrow \Rightarrow \bar{p} \uparrow$
- (no such block recursive solution with discounting)



- benchmark model

$$w = \beta (1 - k)$$

- assumes Nash bargaining and exclusive contracts
  - E must realize project with B that has evaluated
  - removes “hold-up” from revealing information
- or strategic bargaining w/o exog. risk of breakdown (Rubinstein)
  - inside option matters for breaking point, it is zero
- Note: using Nash and no exclusivity, production breaks down
  - analogous to competitive market with fix costs (E gets all output)
  - b/c no search model (no search costs yet)

- flow cost of technology  $a$ :  $\psi(a)$ ,  $\psi'(a) > 0$ ,  $\psi''(a) < 0$ 
  - we specify

$$\psi(a) = \psi^2 + \frac{1}{4}a^2$$

- expected profit flow per unit time (incl. tax  $\tau$ ):

$$\Pi = (1 - \tau) h(b) a \bar{p} (1 - k - w) - \psi(a) \rightarrow \max_a$$

- free entry given optimal technology  $\hat{a}$

$$\Pi(\hat{a}) = 0 \Leftrightarrow h(b) \bar{p} (1 - w - k) (1 - \tau) = \psi$$



4 equations (taken  $w$  as given) determine 4 variables  $\bar{p}$ ,  $R$ ,  $\hat{a}$ ,  $b$

- average productivity (extraction equation)
- E's rational "pricing" of projects (valuation)
- f.o.c. of Bs
- free entry into banking

obtain explicit solution!

# Efficiency measure: GDP



- zero discounting: welfare infinite, use GDP
  - should be identical with risk neutrality
- GDP  $Y$ : steady state flow of output *per unit of time*

$$Y = \underbrace{m(b) \times a \times \bar{p} \times (1 - k)}_{1.} - \underbrace{b \psi(a)}_{2.} - \underbrace{\frac{1 - \bar{p} F}{1 - p R}}_{3.}$$

1. output generated by selected Es
2. cost of running Bs
3. cost of new projects. more complicated.

**Lemma 1** *The flow rate at which E either is selected or arrives at R, which in steady state equals the initial size of all cohorts, equals*

$$\frac{1 - \bar{p}}{1 - p R}$$



- Let's say that the matching function is

$$m(b) = b^\eta$$

- remember, GDP

- all endog. variables solved explicitly: get  $Y = Y(\tau)$ ,  $\left. \frac{\partial^2 Y}{\partial^2 \tau} \right|_{\tau^*} < 0$

## Result 1

$$\tau^* = 1 - \eta = -\frac{\partial h(b)}{\partial b} \frac{b}{h(b)}$$

- CRS ( $\eta = 1$ ): no tax
  - but appropriate to target externalities?
- $\eta < 1$ : tax



- provide intuition for efficiency here
  - understand determinants of  $\tau^*$ , can there be a subsidy?
- no discounting kills important effects
  - characterize model with discounting
  - internalize crowding externality using Hosios
- add losses, variable evaluation costs
- calibrate (?), quantitative relevance?
- anecdotal evidence

# Appendix

# “Wage” determination: no discounting



- Assuming Nash Bargaining with no discounting
  - outside option E (bargaining power  $\hat{\beta}$ ): knows project is good
    - knows will be called eventually, does not discount
    - outside option: will get certain payment  $\hat{w}$  in future
  - outside option B: zero, b/c instantaneous production
    - get nothing, look for another project at zero value
  - split total surplus  $S = 1 - k - \hat{w}$ :

$$(w - \hat{w}) = \hat{\beta} (1 - k - \hat{w})$$

- any rational expectation equ.  $w = \hat{w} \Rightarrow w = 1 - k$
- BUT: there would be no production if Bs get no output
- Thus, our assumption.

# “Wage” determination: with discounting



- discounting introduces real search
- E’s outside option – gives mileage: independent of R

$$D(m(b)a, \delta) \times \hat{w}, \quad D(m(b)a, \delta) \in (0, 1)$$

- incr. meeting rate, less discounting: raises outside option to limit  $\hat{w}$
- rational expectations  $w$  is

$$w = \frac{\beta}{1 + \beta D(m(b)a, \delta)} (1 - k)$$

- no “block recursive” solution because the wage depends on the other endogenous variables
- complexity motivates our simple sharing rule in the benchmark model

# Quality externalities in credit markets: a case for taxing banks?

Christian Bauer & José V. Rodríguez Mora

November 14, 2011